

# Solid Memory: Structural Preferences in Group 2 Dihalide Monomers, Dimers, and Solids

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Abstract: The link between structural preferences in the monomers, dimers, and extended solid-state structures of the group 2 dihalides (MX<sub>2</sub>: M = Be, Mg, Ca, Sr, Ba and X = F, Cl, Br, I) is examined theoretically. The question posed is how well are geometric properties of the gas-phase MX<sub>2</sub> monomers and lower order oligomers "remembered" in the corresponding MX<sub>2</sub> solids. Significant links between the bending in the  $MX_2$  monomers and the  $D_{2h}/C_{3v}$   $M_2X_4$  dimer structures are identified. At the B3LYP computational level, the monomers that are bent prefer the  $C_{3v}$  triply bridged geometry, while the rigid linear molecules prefer a  $D_{2h}$  doubly bridged structure. Quasilinear or floppy monomers show, in general, only a weak preference for either the  $D_{2h}$  or the  $C_{3v}$  dimer structure. A frontier orbital perspective, looking at the interaction of monomer units as led by a donor-acceptor interaction, proves to be a useful way to think about the monomer-oligomer relationships. There is also a relationship between the structural trends in these two ( $MX_2$  and  $M_2X_4$ ) series of molecular structures and the prevalent structure types in the group 2 dihalide solids. The most bent monomers condense to form the high coordination number fluorite and PbCl<sub>2</sub> structure types. The rigidly linear monomers condense to form extended solids with low coordination numbers, 4 or 6. The reasons for these correlations are explored.

## Introduction

Chemistry is well-supplied with instances in which expectations of simplicity are met with real complexity, with experimental observations forcing us to revise ideas on which our intuition is built. The bending observed in the group 2 dihalides is among the most interesting examples of such seemingly counterintuitive behavior. It is now well-known that not all the group 2 dihalide molecules have linear minimum energy structures. In the series  $MX_2$  (M  $\equiv$  Be, Mg, Ca, Sr, Ba; X  $\equiv$  F, Cl, Br, I), the molecules  $CaF_2$ ,  $SrF_2$ ,  $SrCl_2$ , and all the  $BaX_2$ structures are bent.<sup>1-2</sup>

Simple valence bond and molecular orbital models, such as the traditional valence shell electron pair repulsion (VSEPR) model<sup>3</sup> and simple Walsh diagrams,<sup>4</sup> fail to predict this behavior. Since the discovery in the 1960s of this unexpected bending in the group 2 dihalides,<sup>5</sup> various attempts have been made to explain it.6-16 For the most part, these explanations have been

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based on classical electrostatic core-polarization models<sup>7,9,11,15a,16</sup> or hybridization models that take account of the empty (n - n)1)*d* energy level in the heavier metal atoms.<sup>8,10–15</sup> Over the past decade or so, a consensus has gradually emerged that, in fact, both core-polarization and hybridization significantly affect the bonding and structural preferences in these systems.<sup>1,2,12</sup>

An interesting structural diversity has been observed experimentally and computationally in the series of dimers of the group 2 dihalides,  $(MX_2)_2$ , as well. The Be<sub>2</sub>X<sub>4</sub> and Mg<sub>2</sub>X<sub>4</sub> dimers have a  $D_{2h}$  minimum energy structure with two bridging halides, while  $Ca_2F_4$ ,  $Sr_2X_4$ , and  $Ba_2X_4$ , X = F, Cl, feature a  $C_{3v}$ minimum energy geometry with three bridging halides (Figure  $1).^{1,17-21}$ 

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Figure 1. Minimum-energy structural isomers of the groups 2 dihalide dimers.

A question that arises naturally is whether there is a link between the linear/bent structural variation in the monomer and the  $D_{2h}/C_{3v}$  geometrical preference in the dimer. For the systems examined computationally to date, it has been found, in fact, that the monomers that are bent prefer a  $C_{3v}$  dimeric structure, while the linear monomers tend to adopt the  $D_{2h}$  dimer geometry.

Five years ago, Levy and Hargittai performed density functional calculations on six different isomers of Ca<sub>2</sub>X<sub>4</sub>, Sr<sub>2</sub>X<sub>4</sub>, and  $Ba_2X_4$ , X = F and  $Cl^{20}$  They identified for those six systems a correlation between the linear(bent) geometry preference in the monomers and the  $D_{2h}(C_{3v})$  geometry preference in the dimer. Furthermore, they provided computational evidence that, for Ca<sub>2</sub>F<sub>4</sub>, Sr<sub>2</sub>F<sub>4</sub>, Ba<sub>2</sub>F<sub>4</sub> and BaCl<sub>2</sub>, the  $D_{2h}$  conformation is not even a local minimum on the potential energy surface.<sup>20</sup> To the best of our knowledge, however, the Sr and Ba dibromide and diiodide dimers are yet to be fully characterized experimentally or studied using reliable computational methods. Interested in this linear(bent)  $D_{2h}(C_{3v})$  correlation, we have examined a more complete series of the dimer structures to understand better the correspondence between the structural preferences in all 20 monomers and their dimers.

The main subject of this paper is, however, a broader one. We want to know the factors influencing structural proclivities and choices made not only in the dimer but also in higher order oligomers and the extended solids. Ultimately, we would like to better understand how the significantly ionic solids are built up from their simpler building blocks and how well they may *remember* the structural peculiarities of those building blocks.

A systematic analysis of a series of clusters, beginning at the molecule and moving from dimer to trimer etc., would help to answer these questions. Such a study would enable us to see if (and help us to understand how) monomer geometries influence cluster and solid structures. We can do a good job on the dimers, but trimers, tetramers, and other oligomers are likely to be found in a veritable multitude of isomeric local minima. That variability by and large disappears when one gets to the periodic extended solids. So, in this work we will bypass the trimer and higher order oligomer geometries and move directly to examining the solids themselves.

The crystal structures of the solids have been extensively discussed in the literature.<sup>22-24</sup> The structure types exhibited by nearly all the group 2 metal dihalide MX<sub>2</sub> crystals are very well-known: for instance, the rutile structure of  $MgF_2$  and the CaF<sub>2</sub> (fluorite) structure are routinely depicted and analyzed in modern textbooks of structural chemistry.<sup>24</sup> We will show these structures later in this paper.

Structural maps have been developed (for the group 2 dihalides as well as other MX<sub>2</sub> crystal structures) correlating atomic properties of M and X atoms and the MX<sub>2</sub> structure types they adopt.<sup>22,23</sup> These maps have been quite useful in helping solid-state chemists make sense of why a certain combination of M and X atoms may prefer one particular MX<sub>2</sub> structure type over another.

This kind of empirical structural analysis has been carried out for gas-phase molecules, as well. Thus, the bending in group 2 dihalides has been rationalized based on differences in atomic parameters such as valence-orbital radii25 or atomic softness.12,26 As far as we know, however, there has been no attempt to make contact between the arguments explaining geometric variations in the gas phase and the rationalization of the structure profiles (structure types, coordination numbers, etc.) in the solid phases of these dihalides.27

In the present work, we take a first step toward making this connection. We begin by optimizing geometries for the group 2 dihalide monomers and a range of dimer geometries. Correlations between preferred geometries and structural trends in the monomer and dimer structures are identified and examined. The tendencies that are observed in both sets of structures are then compared with the structure type variations in the corresponding MX<sub>2</sub> solids at ambient conditions.

At the end, we discuss how the framework of understanding within which structural variations in the gas phase (monomers and dimers) has been rationalized may more generally inform our understanding of bonding in the solid-phase structures.

# **Theoretical Methods**

Optimized geometries of the monomer and dimer  $(C_{3v} \text{ and } D_{2h})$ structures of the group 2 dihalides have been obtained using the B3LYP28 density functional method and the following basis sets: the 6-311+G\* all-electron basis set was used for Be and Mg; for the larger metal atoms (Ca, Sr, and Ba), we have used the 10-valence electron effective core MWB (WB MEFIT) pseudopotentials and 6s6p5d basis sets developed by the German (Stuttgart and Erlangen) groups.<sup>29</sup> The optimized monomer geometries are sensitive to the d orbital contraction scheme, and uncontracted d-functions have been recommended for the heavier metals.15a,20,29 For this reason, the 6s6p5d basis set with uncontracted d polarization functions have been used. The cc-pVTZ all-electron basis set of Dunning et al.30 has been employed for F and Cl. The latter is unavailable for I and is very expensive computationally for Br; for those halides we have employed the (7-valence electron) effective core MWB pseudopotentials and basis sets.

In addition to being less expensive computationally, the B3LYP method has been shown by Levy and Hargittai<sup>20</sup> to afford reliable geometric and frequency data for monomers and dimers of CaX<sub>2</sub>, SrX<sub>2</sub>, and  $BaX_2$  (X = F, Cl). For comparison, and to augment the data set available for the dimers, all structures have been optimized at the second-order Møller-Plesset, MP2, level of theory, as well, using the said basis sets.31 All our theoretical calculations have been carried out using the Gaussian 03 suite of programs.<sup>32</sup>

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**Table 1.** Structural and Energy Data for the Group 2 Dihalides: Experimental and Computed (B3LYP) Bond Distances *r* and Angles  $\Theta$ ,<sup>*a,b*</sup> Computed Linearization Energies  $E_{\text{lin}} = (E(D_{\odot h}) - E(C_{2\nu}))$ , and Computed Bending Force Constants  $k_{\text{lin}}$  for the Optimized  $D_{\odot h}$  (Linear) Structures

		r/Å <sup>a,c</sup>		Θ/deg <sup>a</sup>	E <sub>lin</sub> /eV	klin/eV rad-2 d
MX <sub>2</sub>	this work	expt	this work	expt	this work	this work
$\begin{array}{c} BeF_2\\ BeCl_2\\ BeBr_2\\ BeI_2 \end{array}$	1.377 1.800 1.961 2.172	1.374(4) 1.791(5) 1.932(11)	180 180 180 180	180 180 180 180		8.717 7.225 5.751 5.221
$\begin{array}{c} MgF_2\\ MgCl_2\\ MgBr_2\\ MgI_2 \end{array}$	1.759 2.186 2.344 2.552	1.746 2.162(5) 2.308(8)	180 180 180 180	180 180 180 180		5.788 6.225 5.120 4.439
$\begin{array}{c} CaF_2\\ CaCl_2\\ CaBr_2\\ CaI_2 \end{array}$	1.996 2.470 2.640 2.857	2.455(8) 2.592(20) 2.822(13)	142.8 180 180 180	142 (1) 180 180 180	0.04	-2.090 0.510 1.114 1.151
$\begin{array}{l} SrF_2\\ SrCl_2\\ SrBr_2\\ SrI_2 \end{array}$	2.130 2.633 2.821 3.040	2.606(8) 2.748(13) 2.990	128.8 152.6 180 180	108 143.3(34) q-linear <sup>b</sup> 180	0.14 0.01	-3.051 -0.702 0.089 0.525
$\begin{array}{c} BaF_2\\ BaCl_2\\ BaBr_2\\ BaI_2 \end{array}$	2.258 2.773 2.973 3.210	2.899(7) 3.130	118.0 126.9 130.4 133.9	100 100; 120(10) 137.1(49) 137.6(9) <sup>f</sup>	0.34 0.13 0.07 0.04	-4.631 -2.571 -2.280 -1.739

<sup>a</sup> Experimental geometries are from refs 1, 36-38, and 43. In ref 1, M. Hargittai has provided an excellent summary of experimental and ab initio geometries that have been obtained for these systems. The experimental errors in brackets are in units of the last significant figure; so, e.g., 137.1(49)  $\leftrightarrow$  137.1  $\pm$  4.9. Bond lengths and bond angles obtained at the MP2 and QCISD computational levels are included in Table S.1. <sup>b</sup> For the so-called quasilinear molecules, the experimental numbers can differ significantly (especially results obtained by matrix isolation IR techniques). For example, in ref 42,  $\Theta(\text{CaF}_2) = 142^\circ$  (argon matrix) and 131° (krypton matrix). For earlier estimates of  $\Theta$  for SrCl<sub>2</sub>, BaBr<sub>2</sub>, and BaI<sub>2</sub>, see ref 41. <sup>c</sup> See refs 40 and 44. In some instances we have been unable to locate reliable experimental values that have been adjusted40 for comparison with the computed geometries. <sup>d</sup> 1 mdyne Å<sup>-1</sup> = 6.241 51 ×  $(r_{\text{linear}}/\text{Å})^2 \text{ eV/radian}^2$ , where  $r_{\text{linear}}$ , the optimized M-X bond distance in the linear geometry, is in Å units. The values of  $r_{\text{linear}}$  and the computed (B3LYP) force constants in mdyne/Å units are given in Table S.2 of the Supporting Information. <sup>e</sup> See ref 15a. <sup>f</sup> See ref 35.

Frequency analysis on the dihalide dimers was necessary in order to characterize the structures we obtained. Levy and Hargittai have already pointed out that at the B3LYP level the default fine grid calculations lead to too many imaginary frequencies and retention of translational contributions.<sup>20</sup> To avoid this pitfall, we have adopted the ultrafine grid, as well, for our frequency calculations.

## Structural Preferences in the Group 2 Dihalide Monomers

The unanticipated bending of the group 2 dihalides is the focus of continued interest in these molecules. The structural variation in the series is quite significant, with bond angles ranging roughly from  $100^{\circ}$  to  $180^{\circ}$  (Table 1), with increased bending as the metal ion gets larger and the halides get smaller (for recent experimental and computational data, see ref 1).

Yielding to a desire to impose order on this small and interesting world of  $MX_2$  molecules, workers have adopted a three-tier classification scheme, categorizing them as linear, quasilinear, and bent. The so-called quasilinear or floppy molecules are those found experimentally to be linear (or bent), but having a relatively low potential energy barrier to bending (or linearization).<sup>2,14</sup> The question of which molecules to put in this category is not easy to answer, as it depends on how conservatively one defines the cutoff linearization (bending) energy. CaF<sub>2</sub>, CaCl<sub>2</sub>, SrCl<sub>2</sub>, and SrBr<sub>2</sub> are structures typically described as quasilinear. Among these, SrBr<sub>2</sub> exhibits the lowest potential energy barrier  $(0.001 \text{ eV})^{15a}$  and is probably the most deserving of the quasilinear label.<sup>1,33</sup> Computed linearization energies (the energy required to make the bent minimum energy structure linear) are shown in column 6 of Table 1. For further discussion on variations in the MX<sub>2</sub> linearization energies and the concept of quasilinearity, see refs 2, 14, 33, and 34.

Aside from a comparison of the potential energy barriers separating the linear and the bent geometries, the relative flexibility of the structures may be assessed by the theoretical bending force constants. The preferred geometry and rigidity (or flexibility) of the  $MX_2$  molecules are characterized by the sign and magnitude of the bending force constant of the linearized structure

$$k_{\rm lin}(\pi) = \left(\frac{\partial^2 U(\Theta)}{\partial \Theta^2}\right)_{\Theta = \pi} = \left(\frac{\partial^2 U(\theta)}{4\partial \theta^2}\right)_{\theta = \pi/2}$$

Here,  $U(\Theta)$  is the molecular potential energy expressed as a function of the X–M–X bond angles,  $\Theta$  (=2 $\theta$ ).  $k_{\text{lin}}$  is positive for linear molecules and is negative for the bent ones. Further, the magnitude of k is a measure of the flexibility of the molecule: the more flexible the molecule is, the smaller the magnitude of k. Hence, the most rigid molecules in the linear (or bent) geometries will have the largest positive (or negative)  $k_{\text{lin}}$  values. Very flexible systems, such as SrBr<sub>2</sub>, will have relatively small (positive or negative) bending force constants. A set of  $k_{\text{lin}}$  values from this work is provided in column 7 of Table 1. The bending force constants listed in Table 1 were obtained directly from our Gaussian 03 calculations (in mdynes  $Å^{-1}$  units) and converted to units of eV rad<sup>-2</sup> (see footnote d of Table 1 for the conversion factor). See Table S.2 (Supporting Information) for values obtained previously by Kaupp et al.<sup>15a</sup> We will return to these quantities later on in the discussion.

Computational (B3LYP) and experimental geometries<sup>1,35–43</sup> of the alkaline earth dihalide molecules are listed in Table 1, as well. Additionally, ab initio data that we have obtained at the MP2 and QCISD levels and values obtained by Kaupp et

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  (39) In ref 1, M. Hargittai has provided a comprehensive review of the experimental structural studies done on the group 2 dihalides before the year 2000. For specific references to experimental studies on individual molecules in the series, see Table 7 of that work.

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<sup>(34)</sup> The term quasilinear is somewhat misleading, implying linearity for all these structures; so, we have accepted the more colloquial but comprehensive description: floppy. The boundaries separating the floppy and the "genuinely" linear or bent molecules are not defined rigorously. Kaupp recently adopted a partitioning scheme based on linearization energies. He described as quasilinear all molecules with energy changes < 4 kJ mol<sup>-1</sup> (~0.04 eV) when deviated by more than 20° around the linear geometry. By that scheme, all the Ca dihalides, SrCl<sub>2</sub>, SrBr<sub>2</sub>, Srl<sub>2</sub>, and Bal<sub>2</sub> qualify as quasilinear.

al.<sup>15a</sup> (QCISD) are included in the Supporting Information (Table S.1). The bending trend is very well established at all three computational levels, with increased bending as the cation gets softer (larger) and the anion gets harder (smaller).<sup>26</sup>

The density functional (B3LYP) bond lengths and angles show reasonable qualitative agreement with the MP2 and QCISD levels of theory and experiment (Table S.1). The B3LYP method tends to exaggerate the bending when compared to those two methods but shows the best overall agreement with the experimental geometries for the dihalides (Table S.1). It must be emphasized here, however, that, for *floppy* (or *quasilinear*) molecules with shallow bending potentials, such as CaF<sub>2</sub>, SrBr<sub>2</sub>, and BaI<sub>2</sub> (0.00 eV  $\leq E_{\text{lin}} \leq 0.04 \text{ eV}$ ),<sup>2,34</sup> the experimental errors are quite large typically. On the computational side, the geometries and bending potentials of floppy molecules are particularly sensitive to the choice of model chemistry (computational method and basis set).<sup>1,2,12,15,44</sup>

The anomalous structural variation in the group 2 dihalide compounds has been extensively discussed in the literature, and a comprehensive review, dedicated in part to models rationalizing the bending trend, has been provided by Kaupp.<sup>2</sup> For the larger cations, the significant bending in the monomer (small  $\Theta$  in Table 1) is favored, since the (n-1)d orbitals are lowlying and  $sd^x$  hybridization is cheaper, compared to  $sp^x$ hybridization.<sup>2,8</sup> Following a classical electrostatic description of the molecules, it has been shown that polarization interactions (including charge-induced dipole and higher order interactions) between the softer cations and the harder anions are enhanced by the bending. And they play a key role in stabilizing the bent Ca, Sr, and Ba dihalide systems as well (see ref 16 and references therein).

Having summarized the structural and energetic data for the monomers, we will turn our attention next to the dihalide dimers.

#### Group 2 Dihalide Dimers: Structural Preferences

As mentioned above, there is an evident correlation between the structures of the MX<sub>2</sub> molecules and their stable dimers.<sup>1</sup> The monomers that are linear dimerize preferentially in the  $D_{2h}$ geometry, but the bent monomers tend to form a triply bridged  $C_{3v}$  dimeric structure (Figure 1). This conclusion has been arrived at slowly and piecewise, however, several groups having contributed over the past decade, examining various parts of the series of dimers experimentally and at various levels of theory.1,17-20,45,46 Furthermore, quantum mechanical or accurate experimental data are unavailable for a few dimers, including  $Sr_2I_4$  and  $Ba_2I_4$ .

In the present work, 10 possible dimer geometries have been studied (see Figure 2), including (i) the  $D_{2h}$  and (ii) the  $C_{3v}$ isomers already mentioned (Figure 1). Geometry optimizations



Figure 2. Possible geometries of the metal dihalide dimers.

have been performed at the B3LYP computational level at reasonable starting points for all 10 geometries (Figure 2). The energies of isomers (ii) to (x) (Figure 2) relative to the  $D_{2h}$ structure,  $\Delta E = E(\text{isomer}) - E(D_{2h})$ , and the number of imaginary frequencies for all the optimized structures are listed in Table S.3 of the Supporting Information.

The relative energies for the four most competitive structures ((i)  $D_{2h}$ , (ii)  $C_{3\nu}$ , (iii)  $C_{2h}(1)$ , and (iv)  $C_{2\nu}(1)$ ) are shown in Table 2. Structures (v)  $C_{2\nu}(2)$ , (vi)  $C_{2\nu}(3)$ , and (vii)  $D_{4h}$  (Figure 2) are significantly higher in energy than the  $D_{2h}$  and  $C_{3v}$  structures. For example, the  $C_{2\nu}(2)$  structure (resulting from an end-on attack of a linear X-M-X on the M atom of its complement) is never competitive. Similarly, the  $C_{2\nu}(3)$  structure is always at high energy, never a local minimum, and for all Be and Mg dihalides, it falls apart to two linear monomers during the optimization procedures. The quadruply bridged  $D_{4h}$  structure (vii), an intriguing possibility, also did not compete well. It was a local minimum only for the Sr and Ba dihalides. There it is +0.10 eV to +0.97 eV above the  $D_{2h}$  isomer, the best performance in the  $D_{4h}$  geometry coming from Ba<sub>2</sub>F<sub>4</sub>, at +0.10 eV.

The final three structures all collapse to one of the other structures. The doubly bridged in-plane cis  $C_{2\nu}(4)$  and trans  $C_{2h}$ -(2) structures all optimize to the  $D_{2h}$  geometry. The  $C_s$  structure is also never a local minima, and the optimization product

<sup>(40)</sup> It is to be emphasized that the direct experimental bond distances have a different meaning from the computational minimum energy geometries (see ref 44) and that the latter have to be corrected for comparisons between theory and experiments to be valid. These corrections have typically not been performed in the old literature. See, e.g., Akishin P. A.; Spiridonov V. P. Kristallografiya **1957**, 2, 475.

<sup>(41)</sup> NIST-JANAF Thermochemical Tables. J. Phys. Chem. Ref. Data; Monograph No. 9, 4<sup>th</sup> ed.; Chase, M. W., Ed.; 1998.
(42) (a) Ramondo, F.; Rossi, V.; Bencivenni, L. Mol. Phys. 1988, 64, 513. (b)

Ramondo, F.; Bencivenni, L.; Cesaro, S. N.; Hilpert, K. J. Mol. Struct. 1989, 192, 83.

<sup>(43)</sup> Hargittai, M. Private communication. Varga, Z.; Lanza, G.; Minichino, C.; (4) Hargittai, M. Hivate communication. Vaga, Z., Lanza, G., Minemio, C., Hargittai, M. Chem. Eur. J., in press.
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(45) Ramondo, F.; Bencivenni, L.; Spoliti, M. THEOCHEM 1992, 277, 171.
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**Table 2.** Relative Energies ( $\Delta E = E(\text{isomer}) - E(D_{2h})$ ) Obtained at the B3LYP Computational Level for the More Competitive Dimer Geometries

		$\Delta E$ /eV $^a$	
dimer	$C_{3\nu}$	$C_{2h}(1)^{b}$	$C_{2\nu}(1)^{b}$
$Be_2F_4$	1.70	$D_{2h}$	$D_{2h}$
Be <sub>2</sub> Cl <sub>4</sub>	1.24	$D_{2h}$	$D_{2h}$
$Be_2Br_4$	1.04	$D_{2h}$	$D_{2h}$
$Be_2I_4$	0.87	$D_{2h}$	$D_{2h}$
$Mg_2F_4$	0.72	$D_{2h}$	$D_{2h}$
Mg <sub>2</sub> Cl <sub>4</sub>	0.67	$D_{2h}$	$D_{2h}$
$Mg_2Br_4$	0.59	$D_{2h}$	$D_{2h}$
$Mg_2I_4$	0.54	$D_{2h}$	$D_{2h}$
$Ca_2F_4$	-0.08	$D_{2h}$	$D_{2h}$
$Ca_2Cl_4$	0.02	$D_{2h}$	$D_{2h}$
$Ca_2Br_4$	0.01	$D_{2h}$	$D_{2h}$
Ca <sub>2</sub> I <sub>4</sub>	0.02	$D_{2h}$	$D_{2h}$
$Sr_2F_4$	-0.32	-0.07	-0.03
$Sr_2Cl_4$	-0.15	$D_{2h}$	$D_{2h}$
$Sr_2Br_4$	-0.12	$D_{2h}$	$D_{2h}$
$Sr_2I_4$	-0.11	$D_{2h}$	$D_{2h}$
$Ba_2F_4$	-0.54	-0.32	-0.23
Ba <sub>2</sub> Cl <sub>4</sub>	-0.32	-0.07	-0.03
$Ba_2Br_4$	-0.28	-0.03	-0.01
Ba <sub>2</sub> I <sub>4</sub>	-0.25	-0.01	0.00

<sup>*a*</sup> Where the  $D_{2h}$  isomer is not the most stable isomer,  $\Delta E$  for the most stable alternative is in bold type. <sup>*b*</sup> Most of the structures collapsed to a slightly distorted  $D_{2h}$  geometry ( $\Delta E = 0.00$  eV).

appears to be quite sensitive to the details of the initial guess geometry. The structures optimized effectively to structure (i), (ii), or (iii) of Figure 2; see Table S.3. The optimized Be<sub>2</sub>I<sub>4</sub> structure is a perturbed  $C_{3\nu}$  ( $C_s$ ) geometry, which is marginally lower in energy compared to the  $C_{3\nu}$  structure (see footnote c in Table S.3 for details).

In Table 2, positive  $\Delta E$  values indicate that the dimer is unstable in the specified geometry relative to the  $D_{2h}$  structure. A negative number indicates that that alternative geometry is more stable than the  $D_{2h}$  structure. For Be, Mg, Ca and most of the Sr dimers, the  $C_{2h}(1)$  and  $C_{2\nu}(1)$  geometries collapsed to an effective  $D_{2h}$  structure, with the terminal halides only very slightly (<1°) out of the plane of the four-membered ring.

The key results of Table 2 may be summarized as follows: The  $D_{2h}$  isomer is the most stable form for Be and Mg dihalides, as well as Ca<sub>2</sub>Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, and Ca<sub>2</sub>I<sub>4</sub>, while the  $C_{3v}$  structure is the most stable geometry for Ca<sub>2</sub>F<sub>4</sub> and all the Sr and Ba dihalides.<sup>47</sup> The  $C_{2h}(1)$  and  $C_{2v}(1)$  variants, (see Figure 2) which could be described as trans and cis bent  $D_{2h}$  structures, compete only when the  $D_{2h}$  structure is unstable. And while they may be local minima, they are thermodynamically unstable with respect to  $C_{3v}$  geometries.

This conformational preference in the dimer structures may be correlated with the linear/bent structural variation in the monomers. The dimers of the bent monomers show the strongest preference for the  $C_{3v}$  arrangement (the most negative  $\Delta E$  values in Table 2). In fact, the  $D_{2h}$  structure is only a transition structure for Ca<sub>2</sub>F<sub>4</sub> and is a second-order saddle point for Sr<sub>2</sub>F<sub>4</sub> and the Ba<sub>2</sub>X<sub>4</sub> dimers (see Table S.3). On the other hand, the dimers of



**Figure 3.** Optimized reaction path for the  $C_{3v} \leftrightarrow D_{2h}$  rearrangements.

the Be and Mg monomers show the strongest preference for the  $D_{2h}$  arrangement (the more positive  $\Delta E$  values in Table 2), with the  $C_{3v}$  structure being a second-order saddle point for Be<sub>2</sub>X<sub>4</sub> (see Table S.3).

The structural linear/bent trend in the molecules does not perfectly match the  $D_{2h}/C_{3v}$  preferences in the dimers. For instance, all the Sr dimers show a preference for the  $C_{3v}$ geometry, even though the SrBr<sub>2</sub> and the SrI<sub>2</sub> monomers are not bent (see Table 1). The difference in energy of the  $D_{2h}$  and  $C_{3v}$  dimer structures  $\Delta E$  is rather low, however: for Sr<sub>2</sub>Br<sub>4</sub>,  $\Delta E = -0.12$  eV, and for Sr<sub>2</sub>I<sub>4</sub>,  $\Delta E = -0.11$  eV (see Table 2).

As mentioned above, the CaF<sub>2</sub> dimer prefers the  $C_{3v}$  structure. The other three CaX<sub>2</sub> dimers show a preference for the  $D_{2h}$  geometry, but  $\Delta E$  is pretty much insignificant for all of them ( $\Delta E \approx 0.01 \text{ eV}$  to 0.02 eV) compared to the other dimers (Table 2, column 2). In fact, by far the most outstanding difference in the  $\Delta E$  data computed at the B3LYP (Table 1) and the MP2 levels (Table S.4, column 2) is the reversal in structural preference of Ca<sub>2</sub>Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, and Ca<sub>2</sub>I<sub>4</sub>. At the MP2 level, the  $C_{3v}$  conformation is more stable than the  $D_{2h}$  one for these structures. However, the computed energy separations are again quite small, being less than 0.1 eV for all four Ca<sub>2</sub>X<sub>4</sub> structures (Table S.4, column 2).

**Interconversion of the Dimer Structures.** We have talked about the difference in energy between the two prevalent dimer geometries, but actually how much does it cost to go from one form to the other? To answer this question we examined a linear transit between the  $C_{3v}$  and  $D_{2h}$  geometries for all four of the CaX<sub>2</sub> dimers using the transition structure optimization facility in Gaussian.<sup>32,48</sup> In each of these calculations, the starting ( $C_{3v}$ and  $D_{2h}$ ) structures were slightly distorted to  $C_s$  symmetry by varying  $\phi$  (Figure 3) by less than 1.0° from its value in the higher symmetry structures. During the optimization procedure, all the coordinates were allowed to vary.<sup>49</sup>

<sup>(47)</sup> Both geometries are local minima on the potential surfaces of Mg<sub>2</sub>X<sub>4</sub>, Ca<sub>2</sub>-Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, Ca<sub>2</sub>L<sub>4</sub>, Sr<sub>2</sub>Cl<sub>4</sub>, Sr<sub>2</sub>Br<sub>4</sub>, and Sr<sub>2</sub>I<sub>4</sub>. For these systems, no imaginary frequency is obtained for either of the two isomers. For the beryllium dihalides, the C<sub>3v</sub> isomer is not a local minimum. Conversely, for the Ca<sub>2</sub>F<sub>4</sub>, Sr<sub>2</sub>F<sub>4</sub>, and BaX<sub>2</sub> structures, the D<sub>2h</sub> structure is not a local minimum (see Table S.3).

<sup>(48)</sup> Foresman, J. B.; Frisch, Æ. Exploring Chemistry with Electronic Structure Methods, 2nd ed.; Gaussian, Inc.; Pittsburgh, PA, 1995–96; Chapter 3, pp 46–49.

<sup>(49)</sup> Regions outside the direct transit between  $C_{3\nu}$  and  $D_{2h}$  in Figure 3 were not computed in the automatic reaction path optimization procedure. The portion of the curves in Figure 3 outside the transit between the  $C_{3\nu}$  and  $D_{2h}$  structures (to the left of the  $C_{3\nu}$  structures in the figure) were computed independently. The structures were optimized for fixed values of  $\phi$  between  $40^{\circ}$  and  $\phi(C_{3\nu})$ .

The calculations were performed at the B3LYP level using the basis sets described in the Theoretical Methods section. For Ca<sub>2</sub>F<sub>4</sub> and Ca<sub>2</sub>Cl<sub>4</sub> the calculations were particularly expensive, since the cc-pVTZ all-electron basis sets were used for the F and Cl atoms, while core pseudopotentials were used for Br and I. For easier convergence, a guessed transition structure was also provided for the Ca<sub>2</sub>F<sub>4</sub> and Ca<sub>2</sub>Cl<sub>4</sub> transits calculations. Furthermore, only seven waypoint structures were optimized along the reaction path for these two dimers; for the heavier dihalides, 10 structures were optimized along the path (Figure 3). In Figure 3, the structural energies have been plotted as a function of  $\phi$ , the angle formed between the two metal sites and the halide that rotates out of the triply bridged region in the " $C_{3v}$ " structure (cf. structures (ii) and (x) in Figure 2) to become a terminal atom in the " $D_{2h}$ " structure (cf. structures (i) and (ii) in Figure 2). Although all the parameters were optimized along the trajectory,  $\phi$  is an ideal reaction coordinate for monitoring the  $C_{3v} \leftrightarrow D_{2h}$  excursion, since it undergoes the most significant change overall, from between 50° and 60° to 180°.

Recall that for Ca<sub>2</sub>Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, and Ca<sub>2</sub>I<sub>4</sub> both geometries are minima on the potential energy surface (Table 2). For these systems, the computed energy barriers are 0.24 eV, 0.22 eV, and 0.21 eV, respectively, for  $C_{3v} \rightarrow D_{2h}$  isomerization (Figure 3), and they are only marginally larger (by 0.01-0.02 eV) for the reverse process  $(D_{2h} \rightarrow C_{3\nu})$ . The interconversion between the two isomers is "allowed"; there are no level crossings along this reaction path. Since the barriers between the  $C_{3v}$  and  $D_{2h}$ isomers are relatively low, and there is only a marginal difference in thermodynamic stability ( $\Delta E$  in Table 2 is small), one might anticipate finding both isomers in the gas phase of Ca2Cl4, Ca2Br4, and Ca2I4. To the best of our knowledge, however, only the  $D_{2h}$  structure has been observed in matrix isolation studies.<sup>42b,50</sup> It would be interesting to effect a rapid quenching from the gas phase in a search for the possible  $C_{3\nu}$ structure.

In the case of Ca<sub>2</sub>F<sub>4</sub>, the kinetic barrier to the  $C_{3v} \rightarrow D_{2h}$ isomerization is 0.30 eV, making the Ca<sub>2</sub>F<sub>4</sub>  $C_{3v}$  structure the most kinetically stable of all the CaX<sub>2</sub> structures in that geometry (see Figure 3). The corresponding barriers for Ca<sub>2</sub>Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, and Ca<sub>2</sub>I<sub>4</sub> (vide supra) are roughly 0.06 eV to 0.09 eV lower. Probably because the actual  $D_{2h}$  isomer is only a transition structure on the Ca<sub>2</sub>F<sub>4</sub> potential energy surface, the automatic  $D_{2h} \leftrightarrow C_{3v}$  structure optimization procedure gives a final product on the  $D_{2h}$  side in Figure 3 in which  $\phi$  is noticeably smaller ( $\phi \approx 165^{\circ}$ ) than the ideal of 180° in the  $D_{2h}$  structure. We have added the data point for the  $D_{2h}$  structure from a separate optimization (unshaded box at the  $D_{2h}$  end of the Ca<sub>2</sub>F<sub>4</sub> trajectory in Figure 3). The optimized  $D_{2h}$  and final transit structures are separated in energy by just 0.002 eV.

Pogrebnaya et al. have also computed the  $C_{3v} \leftrightarrow D_{2h}$  transit for Ca<sub>2</sub>F<sub>4</sub> at the MP2 level previously.<sup>19</sup> The barriers they obtained for both directions (~0.41 eV for  $C_{3v} \rightarrow D_{2h}$  and 0.27 eV for  $D_{2h} \rightarrow C_{3v}$ ) are ~0.1 and 0.05 eV, respectively, larger than the values we find at the B3LYP level (see Figure 3). The computed energy difference between the  $C_{3v}$  and  $D_{2h}$  structures in that work (0.10 eV)<sup>19</sup> is in reasonable agreement, however, with our computed result (0.08 eV; see  $\Delta E$  for Ca<sub>2</sub>F<sub>4</sub> in column 2 of Table 2).

To sum up, the group 2 dihalide dimers,  $M_2X_4$ , exhibit structural preferences that are correlated with the structural preferences in the MX<sub>2</sub> monomers. The relative thermodynamic stability of the  $D_{2h}$  and  $C_{3v}$  structures (see  $\Delta E$  in Table 2) shows a direct correlation with the extent of the bending in and the flexibility of the monomers. The dimers of the molecules that are most bent (BaF<sub>2</sub>, BaCl<sub>2</sub>, BaBr<sub>2</sub>, SrF<sub>2</sub>) have the most stable  $C_{3v}$  structures (Table 2, column 2); the most rigid of the linear molecules (BeX<sub>2</sub> and MgX<sub>2</sub>) show the strongest preference for the  $D_{2h}$  dimer conformation. The energy differences between the isomers are marginal for Ca<sub>2</sub>X<sub>4</sub> X = Cl, Br, and I (Table 2).

It does not take much energy to interconvert the dimer structures; the barrier to  $(C_{3v} \leftrightarrow D_{2h})$  interconversion is between 0.20 eV and 0.25 eV in either direction for all three systems. For Ca<sub>2</sub>F<sub>4</sub>, the  $C_{3v}$  structure is stable relative to the  $D_{2h}$  isomer and is, by all accounts, the global minimum on the potential surface (Table 2, Figure 3).

A Frontier Orbital Perspective on  $MX_2$  Dimerization. The relationship of the monomer ( $MX_2$ ) and dimer ( $M_2X_4$ ) geometries is one of our points of interest. Perhaps another way into their similarities and differences is through a consideration of the dimerization process. Here qualitative frontier orbital considerations may be of value.

The basic idea of frontier orbital molecular orbital (MO) theory is that essential bonding interactions (leading to low kinetic barriers to reaction and thermodynamic stability; unfortunately not very clearly differentiated) will be those maximizing two-orbital two-electron bonding interactions and minimizing two-orbital four-electron antibonding interactions. The maximization or minimization is governed by the perturbation theory expressions for the interaction of two orbitals of energies  $E_i^{\circ}$  and  $E_i^{\circ}$ 

$$\Delta E = \frac{\left|H_{ij}\right|^2}{E_i^\circ - E_j^\circ}$$

with the Hamiltonian  $H_{ij}$  roughly proportional to  $-S_{ij}$ , the negative of the overlap integral.

Many interactions are governed by acid-base interactions (interactions of an acceptor orbital on one component with a donor orbital on the other). Let us trace the consequences of such a perspective for the MX<sub>2</sub> dimerization. We begin with the important valence orbitals (the highest occupied and lowest unoccupied MOs) of a linear and bent MX<sub>2</sub> molecule illustrated in Figure 4.

The diagram is just an approximate representation of the valence orbitals of the group 2 dihalides; we should keep in mind that the contribution of the M and X sites to the orbitals will vary significantly going from Be to Ba and from F to I. As the electronegativity difference between M and X increases, the frontier MOs will be increasingly dominated by the halide contributions. M. Hargittai has pointed out, for instance, that a look at the frontier orbitals of SrCl<sub>2</sub>, far more ionic than the Be and Mg analogues, reveals that the participation of the Sr site is insignificant.<sup>43</sup>

The unusual coefficient pattern in the allylic  $\pi$  orbitals in Figure 4 is due to the relative electronegativity of M and X.

<sup>(50)</sup> Vajda, E.; Hargittai, M.; Hargittai, I.; Tremmel, J.; Brunvoll, J. *Inorg. Chem.* **1987**, *26*, 1171.



*Figure 4.* Representations of the highest occupied MOs (HOMOs) and lowest occupied MOs (LUMOs) in the linear and bent group 2 metal dihalide.

The only essential change on bending is the formation of an "out-pointing" hybrid at M in the LUMO. The high lying donor orbitals are halide p-type lone pair combinations (in and out of plane, with some central M np admixture in some orbitals). The acceptor orbitals are np's localized on M (with important ns hybridization, if bent, as well as some antibonding X lone pair admixture).

The eventual equilibrium dimer geometries are the outcome of optimizing all interactions; perhaps the frontier orbital perspective is most useful in thinking about the early stages of dimerization. Geometries of approach such as (A) in Figure 5 have one good HOMO-LUMO interaction. Geometries such as (B) in Figure 5 symmetrize the situation, leading to two reinforcing frontier orbital interactions. In (C), a bending at M helps the dimer achieve two stabilizing fragment molecular orbital (FMO) interactions.

It is not a far stretch of the imagination to envisage the symmetrization of structures (B) and (C) to the competitive  $D_{2h}$  and  $C_{3v}$  dimer structures. And, just to be fair, we are led to think of approaches (B) and (C) by knowing the product dimer geometries.

We believe that the frontier MO viewpoint provides us with a perspective on how monomer geometries might be related to preferred dimer (or polymer) geometry. If frontier MO interactions are not optimized in an initial dimer geometry, perhaps they might be optimized better if the monomer fragments are allowed to distort (bend). We do not intend to turn this into a quantitative estimate; it is just a way of thinking. Nonetheless, one is led to another question. What are the energy scales of bending (or linearization) vs dimerization? We explore this in the next section.

## **Dimer-Monomer Relationship**

First, let us look in some detail at the geometry of the dimer. The optimized (B3LYP) geometric parameters of the lowest energy ( $D_{2h}$  or  $C_{3\nu}$ ) structure of each dimer are given in Table 3. The corresponding MP2 geometries have been computed, as well, and are summarized in Table S.4 of the Supporting Information. The two sets of computational data show very good qualitative agreement. So, for the rest of our discussion we will focus on the DFT (B3LYP) values in Table 3. The vibrational frequencies obtained at the B3LYP level for all the  $D_{2h}$  and  $C_{3v}$  dimer structures are included in the Supporting Information as well (Table S.5a,b).

The linear conformation exhibited in the gas phase by some of the dihalides is, of course, lost in the dimers. The  $D_{2h}$  structures (see Table 3) may be viewed as an in-plane combination of two monomers each with bond angle  $\alpha$ . This angle is in the range  $128^{\circ} < \alpha < 138^{\circ}$  for all the stable  $D_{2h}$  structures, and the bridging M-X bonds are almost always ~0.2 Å longer than the terminal M-X bonds (Table 3). In the  $C_{3v}$  structures (see Table 3), the bond angle  $\beta$  between the terminal halide and the bridging halides is similar in magnitude to  $\alpha$  in the  $D_{2h}$  structures:  $128^{\circ} < \beta < 138^{\circ}$ . Within the triply bridged region of the minimum energy  $C_{3v}$  structures, the bond angle  $\gamma$  is, of course, significantly smaller. In Table 3,  $79^{\circ} < \gamma < 92^{\circ}$ , decreasing as M gets larger and X gets smaller.

The need for very small  $\gamma$  angles in the optimized  $C_{3\nu}$  conformation provokes the speculation that this dimer conformation should be disfavored for Be, Mg, and most of the Ca dimers, for the same reasons that a bent geometry is disfavored in their monomers. Similarly, we might speculate the  $C_{3\nu}$  conformation is favored in Ca<sub>2</sub>F<sub>4</sub>, Sr<sub>2</sub>X<sub>4</sub>, and Ba<sub>2</sub>X<sub>4</sub> for the same reason the bent monomer geometry is favored.

But let us examine this argument in greater detail. To do so, two key quantities will be considered. The monomer "preparation" or "deformation" energy  $E_{def}$  is defined as the energy cost of preparing the optimized monomer for dimer formation by changing the bond lengths and angle to those of the MX<sub>2</sub> fragments within the  $D_{2h}$  and  $C_{3\nu}$  dimers. The relevant fragments are illustrated in Figure 6.

In the  $D_{2h}$  isomer, both fragments are identical with M–X bonds of length *a* and *b* and bond angle  $\alpha$ . In the  $C_{3v}$  isomer, one fragment has M–X distances *c* and *d* and bond angle  $\beta$ , while the other fragment has equal M–X bonds of length *e* and bond angle  $\gamma$ . The total deformation energies for the MX<sub>2</sub> fragments of the  $D_{2h}$  and  $C_{3v}$  structures,  $E_{def}(D_{2h})$  and  $E_{def}(C_{3v})$ , are listed in Table 4. The  $E_{def}$  values for the individual fragments are given in Table S.6.

Also included in Table 4 are the counterpoise corrected dimerization energies  $E_{\text{dim}}$  that have been computed for both the  $C_{3v}$  and  $D_{2h}$  isomers:  $E_{\text{dim}} = E^{\text{CP}}(\text{M}_2\text{X}_4) - 2E(\text{MX}_2)$ . In each case (monomer and dimer), of course, the respective minimum energy geometries were used.  $E^{\text{CP}}(\text{M}_2\text{X}_4)$  was obtained by adding the counterpoise correction<sup>51</sup>  $\delta^{\text{CP}}$  to the energy  $E(\text{M}_2\text{X}_4)$  of the optimized dimer structure to correct approximately for basis set superposition errors (BSSE).  $E(\text{MX}_2)$  is the energy of the optimized monomer.

**MX<sub>2</sub> Deformation Energies.** Let us look first at the dependence of the  $D_{2h}$  and  $C_{3v}$  deformation energies (columns 3 and 4 of Table 4) on the atomic number of M and X. All the deformation energies are, of course, positive; in each case we are going from the absolute minimum to some higher energy structure on the monomer potential energy surface. For each metal atom,  $E_{def}$  changes in the order F > Cl > Br > I for both isomers. While this result is simple, the pattern is not easy to

<sup>(51)</sup> The counterpoise correction δ<sup>CP</sup>, and *E<sup>CP</sup>*(M<sub>2</sub>X<sub>4</sub>), were obtained directly from our Gaussian 03 calculations. The definition of δ<sup>CP</sup> and steps involved in calculating it are outlined in: Jensen, F. *Introduction to Computational Chemistry*, Wiley: New York, 1999; pp 172–173.



*Figure 5.* Possible interactions leading to  $D_{2h}$  and  $C_{3v}$  dimer formation.



	•		<sup>b</sup>	$\gamma e$						
Dimer	a	b	α	с	d	е	β	γ		
$\mathrm{Be}_{2}\mathrm{F}_{4}$	1.382	1.566	134.4	1.381	1.787	1.498	131.8	100.7		
$\mathrm{Be}_{2}\mathrm{Cl}_{4}$	1.827	2.006	129.9	1.824	2.265	1.936	127.4	107. <b>3</b>		
$\mathrm{Be}_{2}\mathrm{Br}_{4}$	1.994	2.176	129.3	1.991	2.446	2.102	126.1	109.0		
$\mathrm{Be}_{2}\mathrm{I}_{4}$	2.213	2.388	128.5	2.211	2.669	2.309	124.5	111.2		
$Mg_2F_4$	1.762	1.914	139.0	1.772	2.056	1.860	133.0	88.9		
$Mg_2Cl_4$	2.192	2.374	133.6	2.203	2.570	2.307	128.9	97.3		
$Mg_2Br_4$	2.354	2.543	132.8	2.364	2.755	2.473	127.9	99.2		
$Mg_2I_4$	2.566	2.764	131.1	2.575	2.993	2.685	126.4	102.0		
<b>A D</b>										
$Ca_2F_4$	1.996	2.187	141.0	2.008	2.302	2.087	135.8	83.6		
$Ca_2CI_4$	2.452	2.664	136.5	2.465	2.803	2.562	131.4	90.6		
$Ca_2Br_4$	2.625	2.834	136.0	2.638	2.979	2.738	130.3	91.8		
$Ca_2I_4$	2.845	3.057	134.1	2.860	3.212	2.960	128.6	94.5		
Sr E		2 2 / 7			~		1260			
$Sr_2r_4$	2.152	2.347	142.0	2.167	2.455	2.235	136.9	81.1		
Sr <sub>2</sub> Cr <sub>4</sub>	2.622	2.837	137.9	2.639	2.964	2.722	132.7	87.8		
Sr <sub>2</sub> Dr <sub>4</sub>	2.802	3.013	137.0	2.817	3.148	2.908	131.7	88.8		
51214	3.025	3.241	133.0	3.040	3.383	3.135	129.9	91.7		
Ba <sub>2</sub> F <sub>4</sub>	2 295	2 519	1424	2 310	2 631	2 388	138.4	78 7		
Ba₂Cl₄	2 791	3 027	139.0	2.810	3 146	2.300	134.2	84 9		
$Ba_2Br_4$	2.985	3 207	1391	3 001	3 332	3 089	133.5	85.4		
$Ba_2I_4$	3.212	3.441	137.2	3.230	3.571	3.323	131.5	88.3		

<sup>&</sup>lt;sup>*a*</sup> See the Theoretical Methods section for the basis sets used. The geometries for the higher energy dimer structure are in italics.

explain. Deformation involves a *decrease* in the  $X^{\underline{e}}M^{\underline{e}}X$ bond angle in instances where the monomer bond angle,  $\Theta$ , is larger than the angles in dimer fragments. However, an *increase* in the bond angle is necessary when the monomer is bent already (e.g., BaF<sub>2</sub>), so that  $\Theta$  is smaller than  $\alpha$  or  $\beta$ . Furthermore, bond length changes required in going from the monomer to the prepared fragment, such as the stretching of the monomer bond to match *b* and *d* (cf. Table 1 and Table 3), must also be considered.



**Figure 6.** Illustration of MX<sub>2</sub> monomer fragments for which the deformation energies  $E_{\text{def}}$  have been computed (see Table 4): (a) the X<sup><u>a</u></sup>M<sup><u>b</u></sup>X fragment, bond angle =  $\alpha$ , in the  $D_{2h}$  structure, and (b) X<sup><u>c</u></sup>M<sup><u>d</u></sup>X, bond angle =  $\beta$  and X<sup><u>c</u></sup>M<sup><u>c</u></sup>X, bond angle =  $\gamma$  in the  $C_{3\nu}$  structure.

For the X<sup>e</sup>M<sup>e</sup>X fragment in  $C_{3\nu}$  structure,  $\gamma$  is always smaller than  $\Theta$ . So it is easier to identify relationships between the deformation energies of this fragment and the extent of the angle and distance changes required to prepare the monomer fragments for bonding. We observe, in fact, that  $E_{def}$  for this fragment (column 6 in Table S.6) varies indirectly with  $\gamma$ ; that is, the structures with the smallest bond angles require the largest deformation energies.

We mentioned in our initial discussion of the monomers (vide supra) that as M gets larger and softer, bending of the MX<sub>2</sub> monomer becomes less expensive and even pays off for the larger cations.<sup>26</sup> We have therefore not been surprised by a general decrease in the value of  $E_{def}(C_{3v})$  going from M = Be to M = Ba (column 4, Table 4), since the preparation of the X<sup>e</sup>M<sup>e</sup>X fragment in particular always involves significant bending. A decrease in the deformation energy as M gets larger is observed in  $E_{def}(D_{2h})$  as well. As mentioned above, the computed energies for the  $D_{2h}$  structures of the heavier metal atoms with bent monomers are more difficult to interpret. Nonetheless, the decrease in the energy cost of preparing the  $D_{2h}$  fragment (whether by reducing or enlarging the monomer bond angle) is consistent with the view that the softer the metal atom is, the easier it is for any deformation of the structure (in bond length or bond angle) to occur.

Next we have to consider the differences in the magnitude of  $E_{def}(C_{3\nu})$  and  $E_{def}(D_{2h})$  and the possible implications for geometric preferences in the dimer. First, the deformation energies  $E_{def}$  (Table 4) for the  $D_{2h}$  structure are always lower than the deformation energies for the  $C_{3\nu}$  structures. This is the case even where the  $C_{3\nu}$  structure is the more stable isomer! For instance, although the BaF<sub>2</sub>  $C_{3\nu}$  dimer is more stable (by 0.54 eV; Table 2), the energy cost to prepare the MX<sub>2</sub>  $C_{3\nu}$  dimer fragments ( $E_{def}(C_{3\nu}) = 1.24$  eV; Table 4) is nearly twice the

**Table 4.** Computed Energies for the Rearrangement (Deformation) of Pairs of Stable  $MX_2$  Monomers to the Conformations Observed in the  $(D_{2h} \text{ and } C_{3v}) M_2X_4$  Dimers  $E_{def}$ ,<sup>a</sup> and the Counterpoise Corrected Dimerization Energies  $E_{dim} = (E^{CP}(M_2X_4) - 2 \times E(MX_2))^{b,c}$ 

		E <sub>def</sub>	/eV	E <sub>dim</sub> /eV		
preferred isomer		$E_{def}(D_{2h})$	$E_{def}(C_{3v})$	$E_{dim}(D_{2h})$	$E_{dim}(C_{3v})$	
$\begin{array}{c} Be_2F_4\\Be_2Cl_4\\Be_2Br_4\\Be_2I_4\end{array}$	$egin{array}{c} D_{2h} \ D_{2h} \ D_{2h} \ D_{2h} \ D_{2h} \end{array}$	1.87 1.72 1.56 1.44	4.15 3.24 2.85 2.54	-1.26 -0.73 -0.60 -0.45	0.49 0.53 0.47 0.45	
$\begin{array}{c} Mg_2F_4\\ Mg_2Cl_4\\ Mg_2Br_4\\ Mg_2I_4 \end{array}$	$D_{2h} \ D_{2h} \ D_{2h} \ D_{2h} \ D_{2h} \ D_{2h}$	0.94 1.02 0.96 0.93	2.76 2.28 2.05 1.86	-2.43 -1.48 -1.23 -1.00	-1.67 -0.78 -0.64 -0.44	
$\begin{array}{c} Ca_2F_4\\ Ca_2Cl_4\\ Ca_2Br_4\\ Ca_2I_4 \end{array}$	$C_{3 u} \ D_{2h} \ D_{2h} \ D_{2h} \ D_{2h}$	0.43 <b>0.43</b> <b>0.40</b> <b>0.41</b>	<b>1.44</b> 1.21 1.09 1.01	-2.60 - <b>1.97</b> - <b>1.80</b> - <b>1.59</b>	- <b>2.62</b> -1.92 -1.75 -1.53	
$\begin{array}{c} Sr_2F_4\\Sr_2Cl_4\\Sr_2Br_4\\Sr_2I_4\end{array}$	$C_{3v}\ C_{3v}\ C_{3v}\ C_{3v}\ C_{3v}$	0.46 0.30 0.28 0.30	1.26 0.96 0.89 0.83	-2.40 -2.02 -1.86 -1.66	-2.69 -2.14 -1.96 -1.74	
$\begin{array}{c} Ba_2F_4\\ Ba_2Cl_4\\ Ba_2Br_4\\ Ba_2I_4 \end{array}$	$C_{3v}\ C_{3v}\ C_{3v}\ C_{3v}\ C_{3v}\ C_{3v}$	0.69 0.34 0.23 0.21	1.24 0.83 0.69 0.60	-1.87 -1.81 -1.78 -1.64	$\begin{array}{r} -2.43 \\ -2.10 \\ -2.03 \\ -1.91 \end{array}$	

<sup>*a*</sup>  $E_{def}(D_{2h}) = 2[E(X^{\underline{a}}M^{\underline{b}}X; \angle = \alpha) - E(X^{\underline{r}}M^{\underline{r}}X; \angle = \Theta)]$  for the  $D_{2h}$  structure. Similarly,  $E_{def}(C_{3\nu}) = [E(X^{\underline{c}}M^{\underline{d}}X; \angle = \beta) + E(X^{\underline{c}}M^{\underline{c}}X; \angle = \gamma)] - 2E(X^{\underline{r}}M^{\underline{r}}X; \angle = \Theta)$  for the  $C_{3\nu}$  structure (see Figure 6);  $\angle \equiv$  bond angle. <sup>*b*</sup> The correction for basis set superposition errors has been accomplished by the addition of a counterpoise correction to the computed energy  $E(M_2X_4)$ , so  $E^{CP}(M_2X_4) = E(M_2X_4) + \delta^{CP}$ . The counterpoise correction,  $\delta^{CP}$ , and  $E(M_2X_4)$  were obtained at the same computational level (see Theoretical Methods section). <sup>*c*</sup> The values of  $E_{def}$  and  $E_{dim}$  for the preferred structures are in bold type.

cost of preparing the MX<sub>2</sub> fragments of the  $D_{2h}$  dimer ( $E_{def}$ -( $D_{2h}$ ) = 0.69 eV; Table 4). The variation in the deformation energies, therefore, does not by itself explain the  $D_{2h}/C_{3\nu}$  structural preferences in the dimers.

**Dimerization Energies and Structural Preferences.** The outcome of a destabilization in preparing the MX<sub>2</sub> monomer for its geometry in the dimer plus the stabilization upon dimerization is the dimerization energy ( $E_{\text{dim}}$ : columns 5 and 6 of Table 4). This quantity is generally negative for both the  $D_{2h}$  and  $C_{3\nu}$  dimers, indicating that the dimer is stable relative to monomers. Only for the beryllium dimers in the  $C_{3\nu}$  geometry are the dimerization energies positive;  $E_{\text{dim}} \approx +0.5 \text{ eV}$  in each case! Dimerization in the strained  $C_{3\nu}$  geometry does not in the end pay off for the beryllium dihalides. For all the other systems, both the  $D_{2h}$  and  $C_{3\nu}$  dimers are stable relative to the monomers, with the more stable of the two dimers having the more negative dimerization energy (values in bold in columns 5 and 6 of Table 4).

A comparison of the dimerization energies and the deformation energies in Table 4 enables us to rationalize the structural preferences in the dimer and to better understand the link to the bending in the monomer. The strong preference for the  $D_{2h}$ structure in the beryllium dimers is explained by the quite large deformation energies needed to prepare the BeX<sub>2</sub>  $C_{3v}$  fragments compared to the deformation energies for the BeX<sub>2</sub>  $D_{2h}$ fragments (Table 4). The stabilization during the formation of the Be<sub>2</sub>X<sub>4</sub>  $C_{3v}$  dimer is too small to compensate for the large deformation energy. For the magnesium dihalides, the deformation energies are smaller than they are for the beryllium dihalides, and the stabilization upon dimerization is large enough for both the  $D_{2h}$  and  $C_{3\nu}$  isomers to be stable relative to the monomers ( $E_{\text{dim}}$  negative for both isomers). Nonetheless, the  $D_{2h}$  isomer, which has the smaller deformation energy, is more stable than the  $C_{3\nu}$  form.

The geometric preferences in the beryllium and magnesium dimers are explained by the large deformation energies and weak stabilization of the  $C_{3v}$  structure. But how to explain the emergence of a preference for the  $C_{3v}$  structure as M gets larger? As mentioned previously,  $E_{def}(C_{3v})$  is larger than  $E_{def}(D_{2h})$  for all the dimers. However, both  $E_{def}(C_{3v})$  and  $E_{def}(D_{2h})$  decrease going from Be to Ba, and this is accompanied by a significant stabilization of the  $C_{3v}$  isomers relative to the  $D_{2h}$  isomer.

This stabilization is evident from the sharp reduction in the gap between the  $D_{2h}$  and  $C_{3\nu}$  dimerization energies as M gets larger. For instance, the difference between  $E_{\text{dim}}(C_{3\nu})$  and  $E_{\text{dim}}(D_{2h})$  for BeF<sub>2</sub>, MgF<sub>2</sub>, and CaF<sub>2</sub> is 1.75 eV, 0.76 eV, and -0.02 eV, respectively (see columns 5 and 6 of Table 4), the negative sign on the last number indicating that the CaF<sub>2</sub>  $C_{3\nu}$  isomer is more stable than the  $D_{2h}$  isomer. Dramatic reductions in  $E_{\text{dim}}(C_{3\nu}) - E_{\text{dim}}(D_{2h})$  are observed going from BeX<sub>2</sub> to CaX<sub>2</sub> (X = Cl, Br, and I) as well. We have pointed out already, in fact, that the  $D_{2h}$  structures of Ca<sub>2</sub>Cl<sub>4</sub>, Ca<sub>2</sub>Br<sub>4</sub>, and Ca<sub>2</sub>I<sub>4</sub> are not separated from their  $C_{3\nu}$  isomers by much.

For the larger (Sr and Ba) metals, the  $C_{3v}$  structures win out  $(E_{\dim}(C_{3v}) < E_{\dim}(D_{2h}))$  for all the dimers. Even though the strontium bromide and iodide monomers are linear, the stabilization on forming the  $C_{3v}$  structure is enough to compensate for the cost of the significant bending and bond length variations that are necessary to stabilize the  $C_{3v}$  isomer relative to the  $D_{2h}$  structure.

To sum up this section, the deformation energies,  $E_{def}$ , play a decisive role in dimer formation and are responsible in large part for the strong preference for the  $D_{2h}$  structure in Be<sub>2</sub>X<sub>4</sub> and Mg<sub>2</sub>X<sub>4</sub>. This interpretation is in line with the strong preference in the BeX<sub>2</sub> and MgX<sub>2</sub> monomers for a linear geometry.  $E_{def}$  loses significance for the larger cations, however. To begin with, some of the heavier dihalides are already quite bent, and for the floppy (bent and linear) molecules dimerization in the  $C_{3\nu}$  geometry is typically more feasible, as it allows better orbital overlap and interactions leading to bond formation at only a small cost.

A complete correspondence between linear(bent) monomer and  $D_{2h}(C_{3v})$  dimer structural preferences is not observed, however. The linear SrBr<sub>2</sub> and SrI<sub>2</sub> monomers, for example, show a relatively weak preference for the  $C_{3v}$  geometry. A simple connection between the monomer and dimer structural preferences can be made nonetheless, if we make reasonable allowances for the more floppy monomers.

**Interactions Influencing MX<sub>2</sub> Dimerization.** As mentioned previously, the bending in the monomers is enhanced by both the involvement of *d* orbitals in the bonding and the polarization of the cationic core by the halide anions.<sup>2,26</sup> We suggest that these influences are of key importance in explaining the dimer structures as well.

In the  $C_{3v}$  structures, the availability of  $sd^x$  hybrid orbitals makes it possible for the metal ions to form the three equivalent polar bonds in the bridge region of the  $C_{3v}$  dimer at relatively

small (<90°) X–M–X angles, an undertaking that would likely be more expensive if only  $sp^x$  hybrid orbitals were available. In the Be and Mg systems, the reverse is true. d orbitals are unavailable, and the cation is  $sp^x$  hybridized.

The structural variation in the dimers has been rationalized from a purely electrostatic viewpoint, also. Gigli et al. have applied a classical polarized-ion model to the (Mg to Ba) dihalide dimers,<sup>17,18</sup> suggesting in 1977<sup>17</sup> that "...polarization effects, mainly the charge-dipole interactions,...may play a similar role in the polymerization process." as they do in the molecule. They predicted, by an electrostatic model, that the  $D_{2h}$  dimer conformation was the minimum energy arrangement (compared to (ii), (iii), (iv), and (vi) in Figure 2) when the cation polarizability is small, as in the Mg<sub>2</sub>X<sub>4</sub> systems.<sup>17,18</sup> They also succeeded in demonstrating the relative stability of the  $C_{3\nu}$ conformation (ii) and structures (iii) and (iv) (Figure 2) compared to the  $D_{2h}$  conformation for dimers with the larger cations and smaller anions.<sup>18</sup>

The structural preferences in the dimers were explained by the polarizability dependence of the dimer formation energy. The small X–M–X angles in the  $C_{3v}$  structures are stabilized by charge-dipole and dipole-dipole interactions between the M and X sites. The strength of these interactions varies directly with the size of the dipoles induced at M, so the stability of the  $C_{3v}$  structure is dependent on the polarizability of M and the charge on the halide sites: the larger the cation polarizability, and the larger the charge separation along the MX bond (the more electronegative X is), the more stable the  $C_{3\nu}$  structure will be. In the systems where the cation is small and not very polarizable, the X- - -X repulsive interactions predominate and the  $D_{2h}$  structure (with two halides, rather than three, in the bridge region) is the preferred conformation.

To sumarize, it is evident that (aside from the energetics of dimerization) the  $D_{2h}/C_{3v}$  structural preferences in the M<sub>2</sub>X<sub>4</sub> systems may be explained qualitatively using a language already familiar to us from earlier work on the linear/bent structural variations in the MX<sub>2</sub> monomers. The preferences in both the monomers and the dimer are explained by the same electronic and electrostatic influences: the availability of d orbitals at M for mixing with the s and p orbitals and core-polarization effects.

## **MX<sub>2</sub> Crystal Structures**

Next we turn our attention to the extended MX<sub>2</sub> crystal structures; these are, of course, the familiar (and thermodynamically stable) forms in which these compounds commonly occur under ambient terrestrial conditions. We start off with a question. To what extent do the interactions that determine the structure of a molecule influence structural preferences in the extended solid? Put another way, does a solid remember the monomer? The question is asked where it is of interest, of course; for molecular crystals we know the answer: "very well". We want a more challenging system, and crystals thought to be largely ionic certainly offer us that. Specifically, we want to examine the preferences in the extended solid-state structures of the group 2 dihalides. These proclivities will be considered in the broader context of the structural preferences in the group 2 dihalide monomers and dimers, which have been considered in preceding sections.

A relevant observation was made by M. Hargittai and Jancsó,<sup>52</sup> who pointed out that dimers were observed in the vapors of various main group and transition metal dihalides only when dimer fragments were identifiable in the corresponding solid. Additionally, the heat of vaporization of the dimer had to be no more than about 0.43 eV (10 kcal/mol) larger than that of the monomer.

The perceptive remarks by Kaupp at the end of his 2001 review of "non-VSEPR" structures<sup>2</sup> are also noteworthy. In that work, he suggested that the factors responsible for the unexpected geometries of the alkaline earth MX<sub>2</sub> and other compounds may account for unusual structural preferencesspecifically, unsymmetrical coordination-in their extended solids as well. He surmised, for example, that the unsymmetrical coordination in the extended solids of some of the heavy alkaline earth dihydrides and dihalides with the PbCl<sub>2</sub> structure type is likely due to the involvement of d orbitals in the bonding and to core polarization. So far, however, a relationship between structural preferences in the gas phase and in the solid phases of the group 2 dihalides has not been examined systematically.

The structure types exhibited by the group 2 dihalides at ambient conditions<sup>23,24,53-56</sup> are summarized in Figure 7. Some of these are well-known: the SiO<sub>2</sub> ( $\beta$ -cristobalite) structure, the rutile  $(TiO_2)$  and the fluorite  $(CaF_2)$  structures. Some of the structure types may be less familiar, such as the SrBr<sub>2</sub> and the SrI<sub>2</sub> structures.

It will become important in drawing a connection to monomer and dimer structures to focus on the coordination environment of the metal atom (see Table 5). The  $BeX_2$  crystals exhibit the diamond-type open structure of the SiO<sub>2</sub>  $\beta$ -cristobalite structure (ref 24b, pp 352, 787) and (SiS<sub>2</sub> type) chains<sup>57</sup> with tetrahedrally coordinated Be centers (see Table 5 and Figure 7a,b). In both structures the coordination number, CN, at the metal sites is 4. The magnesium dihalides and the CaCl<sub>2</sub>, CaBr<sub>2</sub>, and CaI<sub>2</sub> crystals span a range of structure types, all with six-coordinate metal sites: the TiO<sub>2</sub> (rutile) and CaCl<sub>2</sub> types are stacks of edgesharing octahedra,<sup>58</sup> while the CdCl<sub>2</sub> and CdI<sub>2</sub> types are layer structures, with edge-sharing octahedra within each layer (see Figure 7; ref 24).

The remaining structures represent roughly three different structure types. SrI2 has a unique seven-coordinate metal center (Figure 7g),<sup>54</sup> while the others adopt either the 7 + 2 PbCl<sub>2</sub> structure type or the eight-coordinate fluorite structure (see Figure 7h,i, and Table 5).<sup>56</sup> Note that SrBr<sub>2</sub> is sometimes classified simply as having the PbCl<sub>2</sub> structure type (e.g., ref 23, p 2911) but is probably better described as a significantly distorted PbCl<sub>2</sub> structure (ref 24b, p 378; ref 53). More recently, the structure has been described by Smeggil and Eick as a hybrid of the SrCl<sub>2</sub> and SrI<sub>2</sub> structures. Based on their single crystal

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(54) Rietschel, V. E. Th.; Bärnighausen, H. Z. Anorg. Allg. Chem. 1969, 368,

<sup>(55)</sup> Smeggil, J. G.; Eick, H. A. Inorg. Chem. 1971, 10, 1458. The crystal structure of SrBr<sub>2</sub> was found to be consistent with the P4/n space group. (56) Pies, W.; Weiss, A. In Crystal Structure Data of Inorganic Compounds –

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Troyanov, S. I. Russ. J. Inorg. Chem. 2000, 45, 1481; Zh. Neorg. Khim. (57)2000, 45, 1619.

<sup>(58)</sup> The TiO<sub>2</sub> (rutile) and CaCl<sub>2</sub> structures are homeotypic; TiO<sub>2</sub> is tetragonal (space group P42/mnm), while CaCl2 is orthorhombic (space group Pnnm).



*Figure 7.* Structure types of the group 2 metal dihalide crystals.

*Table 5.* Structure Types and Metal Coordination Numbers (CNs) for Group 2 Dihalide Extended Solids at Ambient Conditions

crystal	type	CN
BeF <sub>2</sub>	SiO <sub>2</sub>	4
BeCl <sub>2</sub> , BeBr <sub>2</sub> , BeI <sub>2</sub> ,	$SiS_2$	4
$MgF_2$	TiO <sub>2</sub>	6
MgCl <sub>2</sub>	CdCl <sub>2</sub>	6
$MgBr_2, MgI_2, CaI_2$	CdI <sub>2</sub>	6
$CaCl_2$ , $CaBr_2$	CaCl <sub>2</sub>	6
$\mathrm{SrI}_2^a$	$SrI_2$	7
SrBr <sub>2</sub> , <sup>b</sup> BaBr <sub>2</sub> , BaI <sub>2</sub>	PbCl <sub>2</sub>	7 + 2
CaF <sub>2</sub> , SrF <sub>2</sub> , SrCl <sub>2</sub> , BaF <sub>2</sub> , BaCl <sub>2</sub> <sup>c</sup>	CaF <sub>2</sub>	8

<sup>*a*</sup> Unique structure; see Figure 7.<sup>54</sup> <sup>*b*</sup> SrBr<sub>2</sub> has been described as a distorted PbCl<sub>2</sub><sup>24b,53</sup> and, more recently, as a hybrid of the SrCl<sub>2</sub> (fluorite) and SrI<sub>2</sub> structures with seven- and eight-coordinate Sr sites.<sup>55 *c*</sup> A PbCl<sub>2</sub> modification of BaCl<sub>2</sub> has been observed at ambient conditions, as well.<sup>56,59</sup> Note that both the fluorite (CaF<sub>2</sub>) (CN = 8) and the PbCl<sub>2</sub> (CN = 7 + 2) modifications are high coordination structure types.

X-ray diffraction data, the Sr atoms are seven- and eightcoordinate, while the Br atoms are trigonally and tetrahedrally coordinated.<sup>55</sup> In the following sections  $SrBr_2$  will be grouped with the regular PbCl<sub>2</sub>, since the coordination number at Sr in  $SrBr_2$  (CN = 7 and 8) coincide with the 7 + 2 coordination in the PbCl<sub>2</sub> structures. Table 6 presents an overview of the structural preferences in the MX<sub>2</sub> monomers (bent or linear), the dimers ( $D_{2h}$  or  $C_{3v}$ ), and the extended solid structures. A simple color coding system has been employed, which distinguishes the fluorite type and lead chloride structure types from the others. The basis for this partitioning will be clarified below.

In preparation for our analysis of the relationship between the molecular (monomer and dimer) structures and the solids, the smallest X-M-X angles (separation between nearest neighbor X sites bonded to the same cation) in each of the nine crystal structures (Figure 7) were examined. The average of these "nearest neighbor" X-M-X angles in the crystal structures are summarized in Figure 8. The bars in the figure have been arranged according to the size of the metal and halide atoms, giving priority to the smallest (lowest atomic number) atoms. The series runs, therefore, from the crystal structures of the Be dihalides (SiO<sub>2</sub> and SiS<sub>2</sub> types), through the (rutile, CdCl<sub>2</sub>) and CdI<sub>2</sub>) magnesium dihalides to the higher coordination structures. Additionally, the lower coordination solids are given priority, so that CaF<sub>2</sub>, which is eight-coordinate, is plotted last. It has been difficult to determine where to position PbCl<sub>2</sub>. The M site in that structure is best described as (7 + 2)-coordinate

Table 6.	Structural F	Preferences i	n the (	Group	2 Dihalide	Gas	Phase	Monomers and	d Dimers,	, and Extended	Solids at	Ambient C	Conditions <sup>a</sup>
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		Be	Mg	Ca	Sr	Ba
	Mol. Structure	Linear	Linear	Bent	Bent	Bent
F	Dimer Structure	$\mathbf{D}_{2\mathrm{h}}$	$\mathbf{D}_{2\mathrm{h}}$	$C_{3v}$	$C_{3v}$	$C_{3v}$
	Structure type	SiO <sub>2</sub>	TiO <sub>2</sub>	CaF <sub>2</sub>	CaF <sub>2</sub>	$CaF_2$
	Mol. Structure	Linear	Linear	Linear	Bent	Bent
Cl	Dimer Structure	$\mathbf{D}_{2\mathrm{h}}$	$\mathbf{D}_{2h}$	$D_{2h}$	$C_{3v}$	$C_{3v}$
	Structure type	$SiS_2$	CdCl <sub>2</sub>	CaCl <sub>2</sub>	CaF <sub>2</sub>	$CaF_2^{b}$
	Mol. Structure	Linear	Linear	Linear	q-linear	Bent
Br	Dimer Structure	$\mathbf{D}_{2h}$	$D_{2h}$	$D_{2h}$	$C_{3v}$	$C_{3v}$
	Structure type	$SiS_2$	$CdI_2$	CaCl <sub>2</sub>	SrBr <sub>2</sub> °	PbCl <sub>2</sub>
	Mol. Structure	Linear	Linear	Linear	Linear	Bent
Ι	Dimer Structure	$D_{2h}$	$D_{2h}$	$D_{2h}$	$C_{3v}$	$C_{3v}$
	Structure type	$SiS_2$	$CdI_2$	$CdI_2$	$SrI_2^{d}$	PbCl <sub>2</sub>

<sup>a</sup> Coordination numbers at M in the extended solids are listed in Table 5. <sup>b</sup> See footnote c in Table 5. <sup>c</sup> See footnote b in Table 5. <sup>d</sup> See Figure 7g.



*Figure 8.* X-M-X angles between nearest neighbor X- --X sites in the MX<sub>2</sub> structure types adopted by the group 2 metal dihalide crystals. The associated coordination numbers and MX<sub>2</sub> solids are listed in Table 5.

rather than nine-coordinate, since two of the halides are further away from M than the other seven. We have chosen to locate  $PbCl_2$ , therefore, between the seven-coordinate  $SrI_2$  structure and the eight-coordinate  $CaF_2$  systems (Figure 8).

The molecules that are linear in the gas phase form solids with CN = 4 or 6 (see Table 5), and with X-M-X angles ranging from the tetrahedral angle in the Be structures to 90° at the octahedrally coordinated Mg and Ca metal centers (Figure 8). The molecules that are bent in the gas-phase condense to give higher coordination solids (Table 5), with smaller X-M-Xangles (between 70° and 80°) (Figure 8). The smallest angle X-M-X angles in the solids (~70.5°) is found in the fluorite structures (Figure 8). This structure type is the one adopted by systems such as SrF<sub>2</sub>, BaF<sub>2</sub>, and BaCl<sub>2</sub> for which the corresponding MX<sub>2</sub> gas-phase monomers (Table 1) and M<sub>2</sub>X<sub>4</sub> dimers (Table 3) exhibit significant bending as well (see blue section in Table 6).

The relationship between the structural variation in the monomer and the solid crystal structures has been examined in further detail by reference to the linearized bending force constant  $k_{\text{lin}}$  of the metal dihalide monomers.

Since  $k_{\text{lin}}$  (see definition above) is sensitive to both the shape and flexibility of the molecule, it is an ideal index to employ in comparing the geometric trends. The bending force constants have a key advantage over the bond angle data in this regard. The bond angle provides no direct information about the degree of flexibility of the molecule, i.e., whether the potential minimum is shallow or deep. For molecules with similar bond angles, the bending force constants may vary over a large range (see Table 1 and Table S.2).

Shown in Figure 9 is a distribution of the  $MX_2$  structure types and coordination numbers of the alkaline-earth dihalide solids at ambient conditions. The coordination numbers for all the structures are indicated in five columns, with one column for all the halides of each metal atom (Be–Ba). In each column, the four structures are spaced along the *y*-direction by the linearized bending force constant (Table 1) of the associated monomer.

In examining the splitting pattern in  $k_{\text{lin}}$  and the variation in the MX<sub>2</sub> crystal structure types (Figure 9), we were surprised by the apparent link between the two sets of data. As indicated in Table 6, as well, the linear gas-phase molecules condense to form either four- or six-coordinate solids. The higher coordination solids are preferred as the monomers become more flexible (as  $k_{\text{lin}} = 0$  is approached), with the unique sevencoordinate SrI<sub>2</sub> and the SrBr<sub>2</sub> structures appearing in this region. Curiously, these two most nontypical MX<sub>2</sub> structure types are derived from two of the most flexible molecules among the group 2 dihalides.

All the CaF<sub>2</sub> (CN = 8) or the PbCl<sub>2</sub> (CN = 7 + 2) structure types fall in the region where  $k_{lin}$  is negative; i.e., only the bent alkaline earth metal halides condense to form the high coordination CaF<sub>2</sub> and genuine PbCl<sub>2</sub> structure types (blue section in Table 6). Hence, a partitioning of the crystal structures on the basis of coordination numbers and/or structure type separates solids for which the associated monomers are linear from those for which the associated monomers are bent.

# A Traceable Connection?

In extended solids, a number of additional interactions that are irrelevant to gas-phase structures become important, such as the van der Waals interactions between layers in the  $CdCl_2$ and  $CdI_2$  structure types (Figure 7). Other interactions are diminished in influences; cation core-polarization effects disappear or become negligible at metal sites with high local

<sup>(59)</sup> Bracket, E. B.; Bracket, T. E.; Sass, R. L. J. Phys. Chem. 1963, 67, 2132.



*Figure 9.* Relationship between structure types (and cation coordination number) in MX<sub>2</sub> crystals and the geometry of MX<sub>2</sub> monomer in the gas phase; CN = 4 (×); CN = 6 (\*); CN = 7 ( $\triangle$ ); CN = 7+2 ( $\bigcirc$ ); CN = 8 ( $\square$ ). The bending force constants used are those listed in Table 1.

symmetry, as in the case of the eight-coordinate metal site in the fluorite structure (Figure 7). One might suppose, therefore, that the influences that are decisive in the monomers and dimers become less significant in higher order oligomers and the solids. Nonetheless, we have found that the linear and the bent monomers condense to form significantly different structure types. Further, the systems that exhibit exceptional behavior in the monomer or dimer forms, such as the very floppy SrBr<sub>2</sub>, show exceptional behavior (a distorted PbCl<sub>2</sub> structure) in the solid phase as well.

We have shown above that although there is an important correlation, the structural variations in the dimers are not directly controlled by the linear/bent structural preferences in the monomer. The dimerization process is highly exothermic, and the dimerization energies are quite large compared to the computed monomer linearization energies (see Tables 1 and 4). Similarly, crystal packing forces in the solids are certainly likely to overcome the relatively weak deformation or preparation energies in the monomers. So, the geometry of the group 2 dihalide monomers, per se, is quite unimportant in determining the structure types of the corresponding solids. But what then is the common thread linking the structural preferences in the monomers, their dimers, and the solids?

As pointed out above, the feasibility of  $sd^x$  hybridization in Ca, Sr, and Ba is believed to be decisive for the geometric patterns in both the monomers and the dimers. The preference for higher coordination in the solids as M gets larger may be explained, as well, by the availability of lower lying *d*-orbitals for bonding. The availability of the (n - 1)d orbitals is important for explaining the high coordination and small angles in the fluorite and PbCl<sub>2</sub> structures, for example. The unavailability

of the *d* orbitals in Be and Mg helps to explain the lower fourand six-coordination in the Be and Mg systems. The increase in CN from  $BeX_2$  to  $BaX_2$  across each row of Table 6 can be rationalized, therefore, in a straightforward manner.

How, though, are the variations down the columns in Table 6 to be explained? The decreased bending of the dihalide molecules as X gets larger has been accounted for partly by the dependence of the sdx-hybridization at M on the electronegativity of X. Based on the work of Cruickshank et al.,60 Coulson pointed out that separation between the s and (n - 1)1)d orbitals in M is expected to decrease as the ionic character of the M-X bond increases.<sup>8</sup> So, participation of the d orbital in bonding is expected to be greatest for X = F and least for X = I. Since the  $s \rightarrow d$  excitation energy decreases anyway in going from Ca to Ba, the influence of the halides on the  $sd^{x}$ hybridization should be more important for Ca compared to Sr and Ba. The electronegativity of X will be more decisive for the involvement of d orbitals in CaX<sub>2</sub> (monomer, dimer or solid) systems than it will be for the SrX<sub>2</sub> and BaX<sub>2</sub> systems. So, for instance, while only  $CaF_2$  is bent in the  $CaF_2$  to  $CaI_2$  series, both SrF<sub>2</sub> and SrCl<sub>2</sub> and all the Ba dihalides are bent.

It is interesting that as we go down the Ca, Sr, and Ba columns in Table 6 the coordination numbers (and structure types) of the solids follow an analogous pattern: only CaF<sub>2</sub> in the Ca series has CN > 7, while SrF<sub>2</sub>, SrCl<sub>2</sub>, SrBr<sub>2</sub>, and all the Ba dihalides have CN > 7. Might the decreased separation of the *s* and *d* orbitals as X gets more electronegative also play a role in rationalizing that behavior?

<sup>(60)</sup> Cruickshank, D. W. J.; Webster, B. C.; Mayers, D. F. J. Chem. Phys. 1964, 40, 3733; 1964, 41, 325 (erratum).

Classically, the decreased coordination number in the Ca structures as X gets larger has been explained in terms of hard sphere repulsion (steric effects) limiting the number of halides that can congregate around a metal center. Pauling's first rule, stipulating a connection between the cation/anion radius ratio and cation coordination number (ref 24a, p 44), is in line with that analysis. The role of  $sd^x$ -hybridization has not been cited before to explain details of the structure type preferences in these or any other system.

## Summary and Outlook

Links between the structural variations of some group 2 dihalide molecules and their dimers have been noted previously. Our desire to probe these connections and to inquire whether the extended solids of the group 2 dihalides ( $BeX_2$  to  $BaX_2$ ) "remember" the gas-phase structures has motivated a comprehensive examination of structural preferences in the monomers, dimers, and solids.

We find some remarkable correlations between the linear-(bent) geometry in the MX<sub>2</sub> monomers, the  $D_{2h}(C_{3v})$  M<sub>2</sub>X<sub>4</sub> structural preferences in the dimer, and the structure type preferences in the MX<sub>2</sub> extended solids.

The rigid linear monomers show a strong preference for forming the  $D_{2h}$  doubly bridged structure and condense to form at ambient conditions extended solids with low coordination numbers CN = 4, 6. The monomers that are bent strongly prefer the  $C_{3v}$  triply bridged dimer geometry and condense to form extended solids (in the PbCl<sub>2</sub> and fluorite structure types) that have high coordination numbers (CN = 7 + 2, 8). The quasilinear or floppy monomers form either the  $D_{2h}$  or the  $C_{3v}$ dimer, with a relatively low barrier separating the two isomers. Two of the very floppy molecules, SrBr<sub>2</sub> and SrI<sub>2</sub>, form unique extended solids at ambient conditions.

The structural preferences in the dimers have been rationalized partly by an MX<sub>2</sub> frontier orbital MO analysis based on  $sp^x$ hybridization. The strong preference for the  $D_{2h}$  structure in the Be and Mg dihalide dimers is explained by the large cost in energy required to deform the linear MX<sub>2</sub> fragments for optimal bonding in the  $C_{3v}$  geometry. The  $C_{3v}$  dimer structure is favored only when the cation is very large, especially when the minimum energy structure of the MX<sub>2</sub> monomer is bent.

The bending in the MX<sub>2</sub> monomer has been explained previously by core-polarization interactions between M and X sites and the availability of *d*-orbitals on M for hybridization with the valence *s* orbitals. We believe the significant stabilization of the  $C_{3\nu}$  geometry for the CaX<sub>2</sub>, SrX<sub>2</sub>, and BaX<sub>2</sub> dimers may be rationalized, as well, both by core-polarization effects, as the metal gets softer going from Be to Ba, and by the availability of *d*-orbitals in Ca, Sr, and Ba.

Polarization effects play a smaller role in the MX<sub>2</sub> extended solids. In addition to the usual rules explaining structure type preferences in ionic solids, we consider that the observed high coordination in CaF<sub>2</sub> and the strontium and barium dihalide solids (Tables 5 and 6) is consistent with the accessibility of the *d*-orbitals at the metal sites and a reduction in the ns-(n-1)d energy separation as X gets more electronegative.

While we are happy with the degree of understanding we have reached, a number of new questions have arisen in this study that deserve further analysis. Given the size and diversity of the structures in the group 2 dihalides, we have been obliged to focus in this work on the set of monomers, dimers, and infinite extended solids. In the future, we would like to consider, as well, the structural preferences (in the gas and solid phases) of transition metal dihalides. In particular, we are interested in examining the bonding patterns in the group 12 dihalides. Much work remains to be done.

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**Supporting Information Available:** Experimental and computed (B3LYP, MP2 and QCISD) minimum energy geometries of the group 2 dihalides; Optimized bond distances for the group 2 dihalides in the linear conformation, linearization energies for the bent dihalides, and the computed bending force constants for the linear molecules; Relative energies obtained at the B3LYP level for all the dimer isomers studied (Figure 2) and the number of imaginary frequencies for each isomer; MP2 geometries of the  $D_{2h}$  and  $C_{3v}$  dimers; B3LYP vibrational frequencies obtained for the  $D_{2h}$  and  $C_{3v}$  dimer structures; Computed deformation (preparation) and dimerization energies ( $E_{def}$  and  $E_{dim}$ ) for the MX<sub>2</sub> fragments of the  $D_{2h}$  and  $C_{3v}$  group 2 dihalide dimers; Complete bibliographic citation of ref 32 in the text. This material is available free of charge via the Internet at http://pubs.acs.org.

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